

For each question, "X" indicates a correct choice.

ANSWER SHEET - BLUE

Question	a	b	c	d	e	Do not write in this column
1				X		
2				X		
3	X					
4			X			
5		X				
6					X	
7				X		
8			X			

ANSWER SHEET - GREEN

Question	a	b	c	d	e	Do not write in this column
1				X		
2					X	
3			X			
4			X			
5		X				
6				X		
7	X					
8				X		

ANSWER SHEET - WHITE

Question	a	b	c	d	e	Do not write in this column
1		X				
2					X	
3			X			
4	X					
5				X		
6			X			
7				X		
8				X		

ANSWER SHEET - YELLOW

For each question, place an "X" in the box of your choice.

Question	a	b	c	d	e	Do not write in this column
1				X		
2		X				
3	X					
4					X	
5				X		
6			X			
7			X			
8				X		

QUESTION SHEET - BLUE

1. If $f(x, y) = e^{\sin x} + x^5y + \ln(1 + y)$, then $\frac{\partial^2 f}{\partial y^2}$ is

(a) $5x^4$ (b) $x^5 + \frac{1}{1+y}$ (c) $20x^3y$ (d) $\frac{-1}{(1+y)^2}$ (e) $e^{\sin x} \cos x + x^5 - \frac{1}{1+y^2}$.

2. The radius of curvature $\rho(s)$ of the helix which is parametrised by $\mathbf{r}(t) = (\cos t, \sin t, t)$ is

(a) $\frac{1}{2}$ (b) $\sqrt{2}$ (c) $1/s$ (d) 2 (e) s .

3. The directional derivative of $f(x, y) = x^3y + 12x^2 - 8y$ at the point $(1, -5)$ in the direction $(3, 4)$ is

(a) $\frac{-1}{5}$ (b) -1 (c) 3 (d) $(9, -7)$ (e) 15 .

4. The value of the triple integral $\iiint_V x^2 - y^2 \, dx \, dy \, dz$ where V is the cylinder whose base is the circle of radius 2 centred at the origin in the xy plane and whose height is 1 is given by

(a) -8π (b) -2π (c) 0 (d) 2π (e) 8π .

5. If $\mathbf{f} = (xyz, yz^2, y + zx^2)$ then $\nabla \times \mathbf{f}$ is equal to

(a) $yz + z^2 + x^2$ (b) $(1 - 2yz, xy - 2zx, -xz)$ (c) $(1 - 2yz, -xy + 2zx, -xz)$
 (d) $(-1 + 2xz, -y + zx, xz)$ (e) $yz + z^2 + x^2 + y$.

6. The line integral $\int_C xy \, ds$ where C is the quarter circle in the xy plane extending from $(2, 0)$ to $(0, 2)$ has value

(a) -1 (b) $\frac{\pi}{2}$ (c) 2 (d) π (e) 4 .

7. The vector field $\mathbf{f} = (2xy - yz + z, x^2 - xz, x - xy)$ is expressible as $\nabla\phi$ where $\phi(x, y, z)$ is

(a) $xyz + x^2$ (b) $xyz + xy$ (c) $xy + yz + zx$ (d) $x^2y - xyz + xz$ (e) $x^2y - xz$.

8. The work done in moving a particle against the force field given by $\mathbf{F}(x, y, z) = (2z, -3x, 5y + 2x)$ along the curve described parametrically by $\mathbf{r}(t) = (t, t^2, t^3)$, $0 \leq t \leq 2$ is

(a) 3 (b) 17 (c) 112 (d) 200 (e) 280 .

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