



UNIVERSITY *of* LIMERICK  
OLLSCOIL LUIMNIGH

Faculty of Science and Engineering  
Department of Mathematics & Statistics

**MID TERM ASSESSMENT PAPER**

MODULE CODE: MA4003

SEMESTER: Autumn 2012/13

MODULE TITLE: Engineering Mathematics 3 DURATION OF EXAMINATION: 45 minutes

LECTURER: Dr. M. Burke

PERCENTAGE OF TOTAL MARKS: 20 %

Colour: Green

**INSTRUCTIONS TO CANDIDATES: Answer all questions. All questions carry equal marks.  
Use the Answer Sheet below.**

ANSWER SHEET

STUDENT'S NAME:

STUDENT'S ID NUMBER:

For each question, place an "X" in the box of your choice.

Question	a	b	c	d	e	Do not write in this column
1		X				
2	X					
3					X	
4				X		
5		X				
6					X	
7				X		
8				X		
9					X	
10			X			

### Table of Laplace Transforms

$f(t), t \geq 0$	$F(s) = \mathcal{L}[f(t)]$
1	$\frac{1}{s}$
$t$	$\frac{1}{s^2}$
$t^n$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\frac{1}{s-a}$
$t^n e^{at}$	$\frac{n!}{(s-a)^{n+1}}$
$\sinh at$	$\frac{a}{s^2-a^2}$
$\cosh at$	$\frac{s}{s^2-a^2}$
$\frac{1}{a-b}(e^{at} - e^{bt})$	$\frac{1}{(s-a)(s-b)}$
$\frac{a}{a-b}e^{at} - \frac{b}{a-b}e^{bt}$	$\frac{s}{(s-a)(s-b)}$
$\sin at$	$\frac{a}{s^2+a^2}$
$\cos at$	$\frac{s}{s^2+a^2}$
$f'(t)$	$sF(s) - f(0)$
$f''(t)$	$s^2F(s) - sf(0) - f'(0)$
$\int_0^t f(\tau) d\tau$	$\frac{1}{s}F(s)$
$e^{at}f(t)$	$F(s-a)$
Heaviside $u_a(t)$	$\frac{e^{-as}}{s}$
$f(t-a)u_a(t)$	$e^{-as}F(s)$
Ramp $R(t-a)$	$\frac{e^{-as}}{s^2}$
$tf(t)$	$-F'(s)$
$\frac{f(t)}{t}$	$\int_s^\infty F(\sigma) d\sigma$
$(f * g)(t) \equiv \int_0^t f(t-\tau)g(\tau) d\tau$	$F(s)G(s)$
$f(t) = f(t+p)$	$\frac{1}{1-e^{-sp}} \int_0^p f(t)e^{-st} dt$

All  $f(t)$  are defined for  $t \geq 0$ .

1. The Laplace Transform of  $\cosh 3t + \sinh 3t$  is

(a)  $\frac{s+3}{s^2+9}$  (b)  $\frac{1}{s-3}$  (c)  $\frac{s}{s^2-3^2}$  (d)  $\frac{1}{s+3}$  (e)  $\frac{s+3}{(s^2+9)^2}$

2. The Laplace Transform of  $e^{2t}(3t+1)$  is

(a)  $\frac{s+1}{(s-2)^2}$  (b)  $\frac{s+3}{(s-2)^2}$  (c)  $\frac{3s+1}{(s+2)(s-2)^2}$  (d)  $\frac{3s+1}{s^2(s-2)}$  (e)  $\frac{s+3}{s^2}e^{-2s}$

3. The Laplace Transform of  $f(t) = \cos(2t-4)u_2(t)$  is

(a)  $\frac{2}{s^2+4}e^{-2s}$  (b)  $\frac{e^{-2}}{s(s^2+4)}$  (c)  $\frac{s}{s^2+4}e^{-s}$  (d)  $\frac{s}{s^2+1}e^{-2s}$  (e)  $\frac{s}{s^2+4}e^{-2s}$

4. The inverse Laplace transform of  $\frac{2}{s^2+4}e^{-s}$  is

(a)  $e^{-4t}u_1(t)$  (b)  $e^{-t}\sin 2t$  (c)  $\sin t u_2(t)$  (d)  $\sin 2(t-1)u_1(t)$  (e)  $e^{-2(t-1)}u_1(t)$

5. The inverse Laplace transform of  $\frac{s-2}{s^2-s-6}$  is

(a)  $e^{-3t}$  (b)  $\frac{4}{5}e^{-2t} + \frac{1}{5}e^{3t}$  (c)  $2e^{-2t} - e^{3t}$  (d)  $\frac{3}{7}e^{-t} + \frac{4}{7}e^{6t}$  (e)  $e^{3t}$

6. The convolution of  $e^t$  with  $e^{-2t}$  (also denoted by  $e^t * e^{-2t}$ ) is given by

(a)  $\frac{1}{3}(-e^t + e^{-2t})$  (b)  $1 - e^{-t}$  (c)  $e^{-2t}$  (d)  $e^{-t}$  (e)  $\frac{1}{3}(e^t - e^{-2t})$

7. The function  $f: \mathbb{R} \rightarrow \mathbb{R}$  satisfies  $f(x+2) = f(x)$ . The period of  $f(x/2)$  is

(a) 1 (b)  $\frac{\pi}{2}$  (c) 2 (d) 4 (e)  $2\pi$

8. The functions  $f(x) = 1 - x^2/2$  and  $g(x) = x^3$  defined on  $-1 < x < 1$  have the property that

(a) both are even (b) both are odd (c)  $f$  is odd and  $g$  is even  
(d)  $f$  is even and  $g$  is odd (e) at least one is neither even nor odd

9. The function  $f(x) = -x$  for  $-\pi < x < \pi$  is periodic with period  $2\pi$ . It has a Fourier Series  $\sum_{n=1}^{\infty} b_n \sin(nx)$ .  $b_2$  is given by

(a) -1 (b)  $-\frac{1}{\pi}$  (c) 0 (d)  $\frac{1}{\pi}$  (e) 1

10. The coefficient  $a_0$  in the Fourier Series for the periodic function  $f(x) = \sinh x$  if  $-1 < x < 1$  with period 2 has the value

(a)  $-2 \cosh 1$  (b) -1 (c) 0 (d)  $2(\cosh 1 - 1)$  (e)  $2 \cosh 1$